

INTRODUCTION

- ▶ **Key Idea:** Guiding diffusion process at each node by a downstream transformer via diffusion-kernel and multi-head attention.
- ▶ **Problem:** Limitations in interpreting the brain networks in a scenario with multiple imaging biomarkers.
 - Convolutional approaches ineffectively aggregate information from distant nodes, while attention-based methods exhibit deficiencies in capturing node-centric information, particularly in retaining critical properties from pivotal nodes.
 - These shortcomings reveal challenges for identifying disease-specific variation from diverse features from different modalities.
- ▶ **Contribution:**
 - Proposing a novel framework to aggregate both short- and long- range properties for better prediction of graph labels.
 - Demonstrating superior performance on graph classification in comparisons to the state-of-the-art methods.
 - Showing interpretability on the brain networks in a scenario with multiple imaging biomarkers.

PRELIMINARY: GRAPH KERNEL CONVOLUTION

- ▶ An undirected graph $G = \{V, E\}$ with N nodes comprises a node set V and an edge set E . A symmetric adjacency matrix A and a diagonal degree matrix D can be computed from E . A graph Laplacian is defined as $L = D - A$. It has a complete set of orthonormal eigenvectors $U = [u_1 | u_2 | \dots | u_N]$ and corresponding real and non-negative eigenvalues $0 = \lambda_1 \leq \dots \leq \lambda_N$, so does the normalized Laplacian $\hat{L} = D^{-1/2} L D^{-1/2}$.

- ▶ From Spectral Graph Theory, the choice of a kernel function determines specific graph characteristics. A heat-kernel between nodes p and q is spanned by U as

$$h_s(p, q) = \sum_{i=1}^N e^{-s\lambda_i} u_i(p) u_i(q) \quad (1)$$

where u_i is the i -th eigenvector. The kernel $e^{-s\lambda_i}$ captures smooth transition between nodes within the scale s as a low-pass filter. Graph Fourier transform, i.e., $\hat{x} = U^T x$, defines the graph convolution $*$ of a signal $x(p)$ with a filter h_s as

$$h_s * x(p) = \sum_{i=1}^N e^{-s\lambda_i} \hat{x}(i) u_i(p) \quad (2)$$

whose band-width is controlled by the scale s .

GNN WITH TRANSFORMER-GUIDED ADAPTIVE DIFFUSION (GTAD)

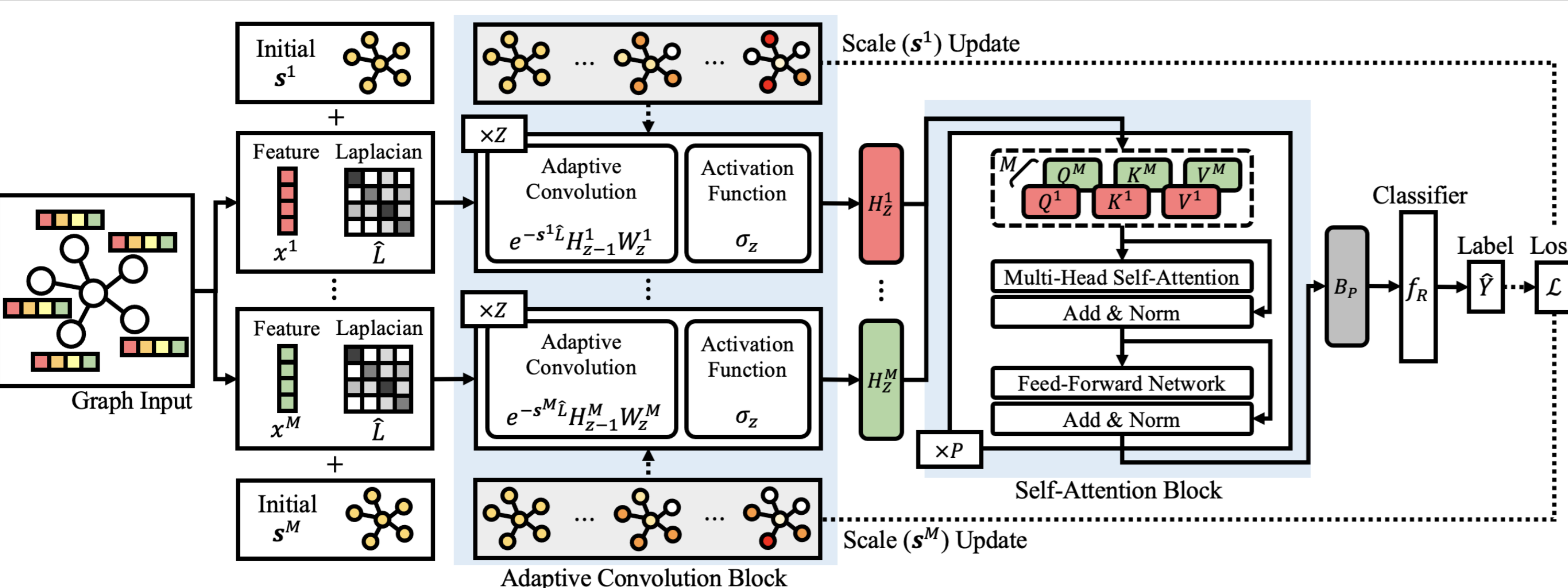


Figure: Illustration of our framework (GTAD). A novel end-to-end framework GTAD that learns node-centric parameters of a diffusion kernel which are governed by a transformer.

- ▶ **Modality-wise Adaptive Convolution Block.** Consider G given as $\hat{L} \in \mathbb{R}^{N \times N}$, a set of features (i.e., imaging measures) $X = \{x^m\}_{m=1}^M$ defined on N nodes from M modalities, a set of trainable scales $\{s^m\}_{m=1}^M$ where $s^m \in \mathbb{R}^N$ and a graph label Y . Each encoder consists of multiple graph convolution layers that adaptively aggregate features for each node with a non-linear activation function σ_z as

$$H_z^m = \sigma_z(e^{-s^m \hat{L}} H_{z-1}^m W_z^m). \quad (3)$$

- ▶ **Modality-wise Self-Attention Block.** The obtained embeddings $\{H_z^m\}_{m=1}^M$ are inputted to an attention block to compute node-wise attention scores. Using the self-attention scores, a self-attention value is computed as

$$\phi(Q^m, K^m, V^m) = \sigma\left(\frac{Q^m K^{mT}}{\sqrt{C}}\right) V^m. \quad (4)$$

- ▶ **Transformer-Guided Scale Update.** To update a scale s_n^m at the n -th node for the m -th encoder, the objective function is defined by cross-entropy between the true value Y_{ij} and the prediction \hat{Y}_{ij} .

$$\mathcal{L} = -\frac{1}{T} \sum_{t=1}^T \sum_{j=1}^J Y_{tj} \ln \hat{Y}_{tj} + \alpha \frac{1}{M} \sum_{m=1}^M \sum_{n=1}^N \mathbb{1}_{s < 0} |s_n^m|. \quad (5)$$

Update of the modality-specific scales is performed as $s \leftarrow s - \beta \frac{\partial \mathcal{L}}{\partial s}$ via gradient-descent with a learning rate β .

ALZHEIMER'S DISEASE NEUROIMAGING INITIATIVE (ADNI)

- ▶ On the same parcellation, region-wise imaging features such as Standard Uptake Value Ratio (SUVR) of metabolic intensity from FDG-PET, β -Amyloid protein from Amyloid-PET and cortical thickness from MRI were measured.
- ▶ Diagnostic labels: Control (CN), Significant Memory Concern (SMC), Early Mild Cognitive Impairment (EMCI)

Table: Demographics of the preclinical ADNI dataset.

Category	CN	SMC	EMCI
# of subjects	333	172	414
Gender (Male / Female)	156 / 177	62 / 110	240 / 174
Age (Mean \pm Std)	73.0 \pm 5.9	71.7 \pm 5.2	71.0 \pm 7.7

CLASSIFICATION RESULT

Table: Preclinical AD classification performance (CN/SMC/EMCI) on ADNI data.

Modalities	Cortical Thickness & β -Amyloid			Cortical Thickness & FDG		
	Accuracy	Precision	Recall	Accuracy	Precision	Recall
GCN	0.861 \pm 0.04	0.772 \pm 0.06	0.780 \pm 0.06	0.873 \pm 0.02	0.802 \pm 0.02	0.813 \pm 0.03
GAT	0.896 \pm 0.01	0.827 \pm 0.03	0.839 \pm 0.02	0.882 \pm 0.02	0.811 \pm 0.03	0.844 \pm 0.03
GraphHeat	0.868 \pm 0.02	0.777 \pm 0.05	0.797 \pm 0.04	0.887 \pm 0.03	0.821 \pm 0.04	0.834 \pm 0.03
GDC	0.858 \pm 0.02	0.767 \pm 0.03	0.786 \pm 0.04	0.842 \pm 0.01	0.743 \pm 0.02	0.765 \pm 0.03
ADC	0.906 \pm 0.02	0.835 \pm 0.03	0.861 \pm 0.04	0.896 \pm 0.01	0.831 \pm 0.01	0.847 \pm 0.02
LSAP	0.911 \pm 0.01	0.847 \pm 0.03	0.872 \pm 0.02	0.934 \pm 0.02	0.899 \pm 0.05	0.904 \pm 0.03
NodeFormer	0.916 \pm 0.02	0.856 \pm 0.04	0.865 \pm 0.02	0.944 \pm 0.01	0.913 \pm 0.03	0.921 \pm 0.02
DIFFormer	0.930 \pm 0.01	0.877 \pm 0.03	0.900 \pm 0.02	0.954 \pm 0.01	0.923 \pm 0.02	0.944 \pm 0.01
SGFormer	0.941 \pm 0.01	0.894 \pm 0.03	0.911 \pm 0.02	0.959 \pm 0.01	0.931 \pm 0.01	0.945 \pm 0.01
GTAD (Ours)	0.945\pm0.02	0.901\pm0.03	0.919\pm0.02	0.963\pm0.01	0.935\pm0.02	0.948\pm0.01

Modalities	β -Amyloid & FDG			All Imaging Features		
	Accuracy	Precision	Recall	Accuracy	Precision	Recall
GCN	0.880 \pm 0.01	0.806 \pm 0.02	0.813 \pm 0.02	0.888 \pm 0.02	0.816 \pm 0.02	0.826 \pm 0.02
GAT	0.877 \pm 0.02	0.815 \pm 0.03	0.814 \pm 0.04	0.912 \pm 0.01	0.858 \pm 0.02	0.864 \pm 0.02
GraphHeat	0.880 \pm 0.02	0.804 \pm 0.05	0.824 \pm 0.03	0.893 \pm 0.02	0.824 \pm 0.03	0.839 \pm 0.03
GDC	0.866 \pm 0.02	0.787 \pm 0.03	0.790 \pm 0.03	0.867 \pm 0.02	0.779 \pm 0.03	0.799 \pm 0.02
ADC	0.910 \pm 0.01	0.865 \pm 0.02	0.856 \pm 0.02	0.904 \pm 0.02	0.855 \pm 0.04	0.858 \pm 0.02
LSAP	0.922 \pm 0.02	0.862 \pm 0.05	0.893 \pm 0.03	0.912 \pm 0.01	0.844 \pm 0.04	0.879 \pm 0.02
NodeFormer	0.931 \pm 0.01	0.887 \pm 0.03	0.893 \pm 0.03	0.938 \pm 0.02	0.900 \pm 0.03	0.902 \pm 0.03
DIFFormer	0.951 \pm 0.01	0.919 \pm 0.03	0.933 \pm 0.02	0.953 \pm 0.01	0.920 \pm 0.02	0.936 \pm 0.02
SGFormer	0.954 \pm 0.01	0.923 \pm 0.03	0.936 \pm 0.02	0.951 \pm 0.01	0.911 \pm 0.02	0.933 \pm 0.02
GTAD (Ours)	0.962\pm0.01	0.935\pm0.02	0.946\pm0.02	0.963\pm0.01	0.943\pm0.01	0.941\pm0.02

INTERPRETATION OF THE TRAINED GTAD

- ▶ **Discussion on the Scales**

- The trained model yields node-wise optimized scales, where each node corresponds to a specific ROI in the brain.

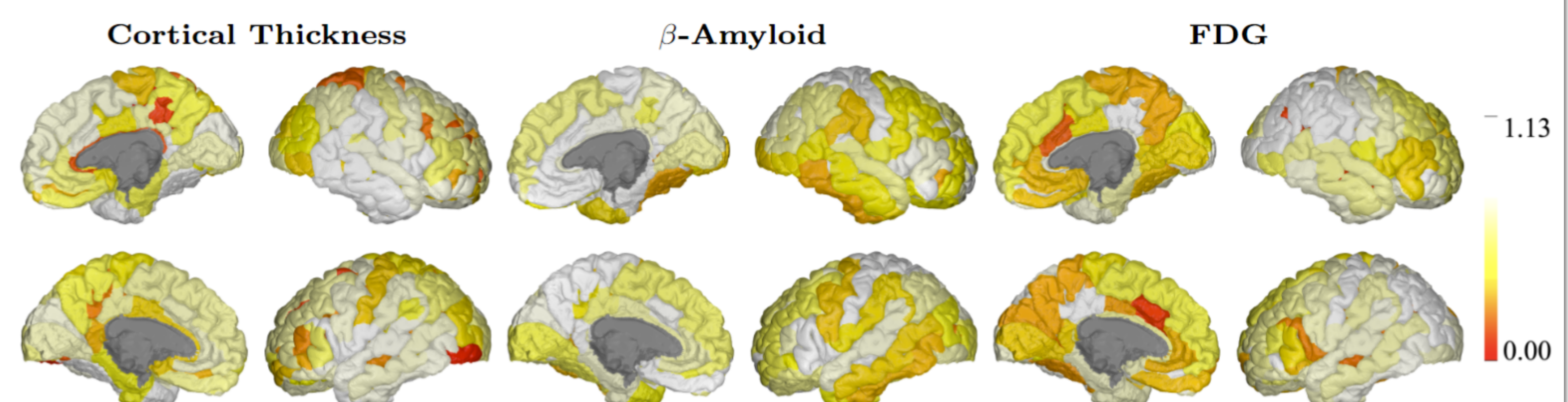


Figure: Visualization of learned scales on the cortical regions of left (top) and right (bottom) hemispheres.

- ▶ **Pre-clinical AD via ROI Attention**

- From the attention block, each ROI gains long-range characteristics from other ROIs by modality-wise attention mechanism.
- Most relevant ROIs in Preclinical AD prediction can be detected by total attention scores that represent the intensity of attention at each ROI in the brain.

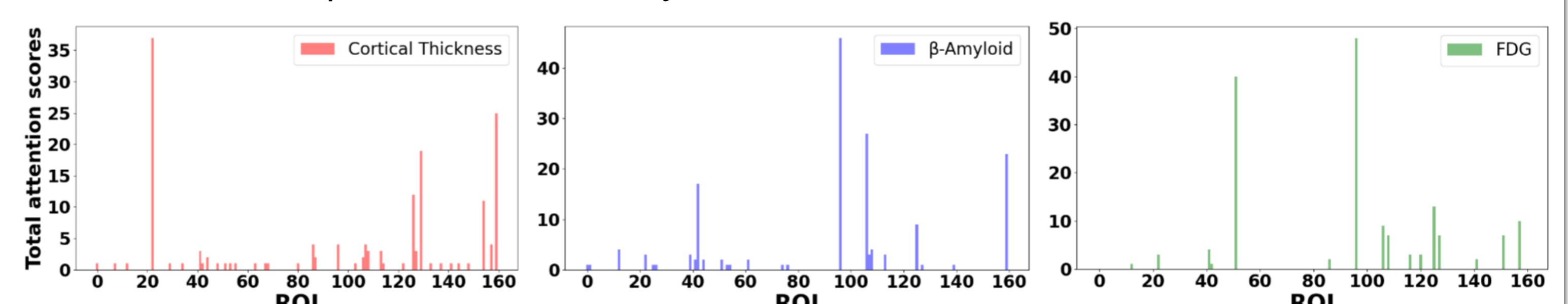


Figure: Distribution of attention scores across all brain regions with cortical thickness (left), β -Amyloid (center) and FDG (right).

- ▶ **Ablation Study on the Blocks**

- To explore the effect of each block, ablation study on convolution types and attention types for preclinical AD classification is given.

Table: Performance comparisons of different blocks. For attention block, our multi-modal (MM) attention and existing position-wise attention are compared.

Convolution Block	MM Attention	Accuracy	Precision	Recall
Multi-Layer Perceptron	✗	0.939 \pm 0.03	0.893 \pm 0.05	0.913 \pm 0.04
	✓	0.947 \pm 0.02	0.906 \pm 0.04	0.933 \pm 0.02
Graph Convolution Layer	✗	0.899 \pm 0.01	0.835 \pm 0.03	0.849 \pm 0.03
	✓	0.900 \pm 0.01	0.834 \pm 0.03	0.852 \pm 0.02
Adaptive Convolution Layer (Ours)	✗	0.945 \pm 0.03	0.903 \pm 0.05	0.922 \pm 0.04
	✓	0.963\pm0.01	0.943\pm0.01	0.941\pm0.02